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Extreme Anomalous Particle Transport in the Random Linear Amplification Model of the Edge Plasma Turbulence.

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The anomalous, or strange character of the particle transport in random environment is characterised by the algebraic asymptotic behaviour of the mean values of powers of particle displacement $\mathbf{r}(t)$ versus time. In the most general case, the anomalous or strange character is encoded in the dependence on p of the exponents $\zeta_p = \lim_{t \rightarrow \infty} \log \left[\langle |\mathbf{r}(t)|^p \rangle \right] / \log(t)$. In the normal case: $\zeta_p = p/2$ [1]. The *extreme anomalous* particle transport studied in this work is characterised by an exponential divergence, in the limit of large times t , of the higher moments of the particle displacement. For $p > \beta \geq 0$, the asymptotic formula hold: $p - \beta = \lim_{t \rightarrow \infty} \log \left[\langle |\mathbf{r}(t)|^p \rangle \right] / t$, in other words for $p > \beta$ and large time t , we have: $\langle |\mathbf{r}(t)|^p \rangle \propto \exp[(p - \beta)t]$. We remark the contrast with usual anomalous case [1], where for large time t we have $\langle |\mathbf{r}(t)|^p \rangle \propto t^{\zeta_p}$.

This new result is demonstrated in the framework of the random linear amplification model described in [2], which was developed to explain the experimental results on the edge turbulence on DIII-D tokamak, from refs. [3-4]. The constant β is the power law decay exponent of the heavy tail of the cumulative probability distribution function of the intensity of electrostatic field fluctuations in the plasma edge [2].

From empirical approximate [4] or exact self-similarity arguments, it follows [2], that $0 < \beta \ll 1$, which is confirmed by tokamak edge plasma measurements [3] as well as by three fundamental self-organized criticality models [5]. It follows that all the integer moments of the particle displacement diverge exponentially, justifying the “*extreme anomalous*” terminology. We proved that the *extreme anomalous* particle transport qualitatively give rise to the correct, experimentally verified, isotope effect.

References.

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